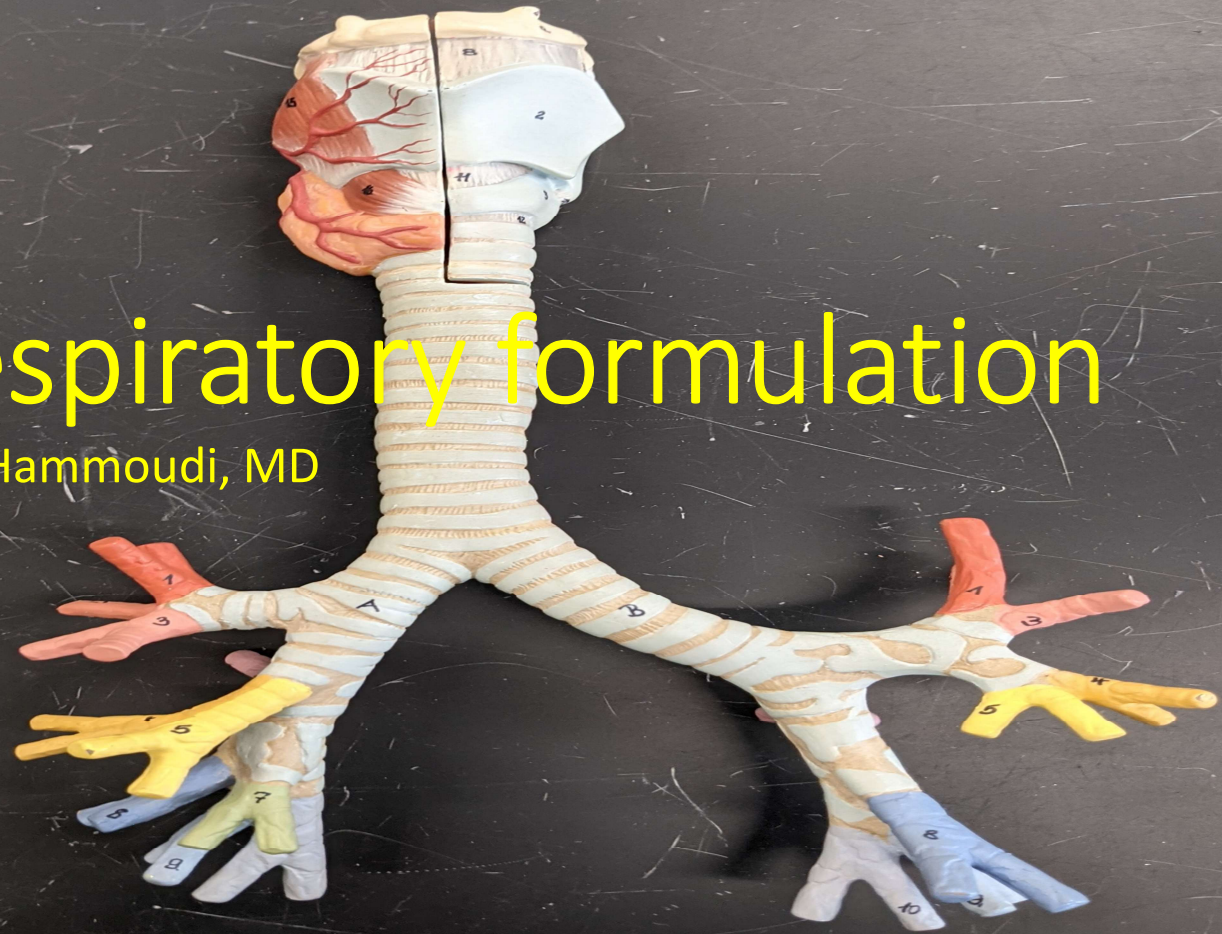


# The respiratory formulation

D.Hammoudi, MD



### **Boyle's Law:**

For a fixed mass of gas at constant temperature, the pressure (P) and volume (V) are inversely proportional, such that  $P \times V = k$ , where k is a constant.

**Physiologic dead space (VD):** volume of inspired air that does not participate in gas exchange  
**VD** is the sum of the anatomic dead space and the alveolar dead space

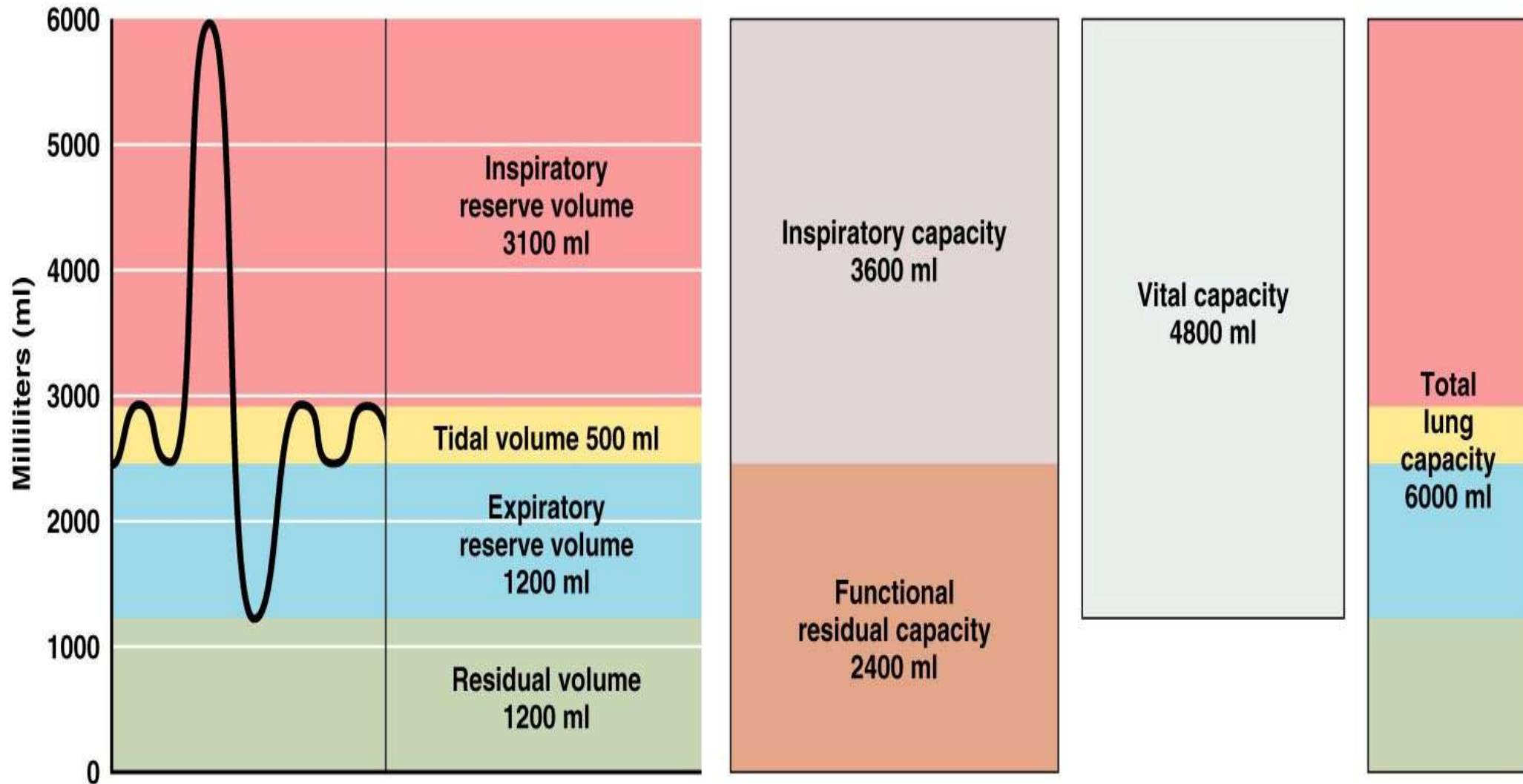
**Anatomic dead space:** the volume of air in the conducting zone, e.g., **mouth, trachea (approx. 1/3 of the resting tidal volume)**

**Alveolar dead space:** the sum of the volumes of alveoli that do not participate in gas exchange (mainly apex of the lungs); These alveoli are ventilated but not perfused

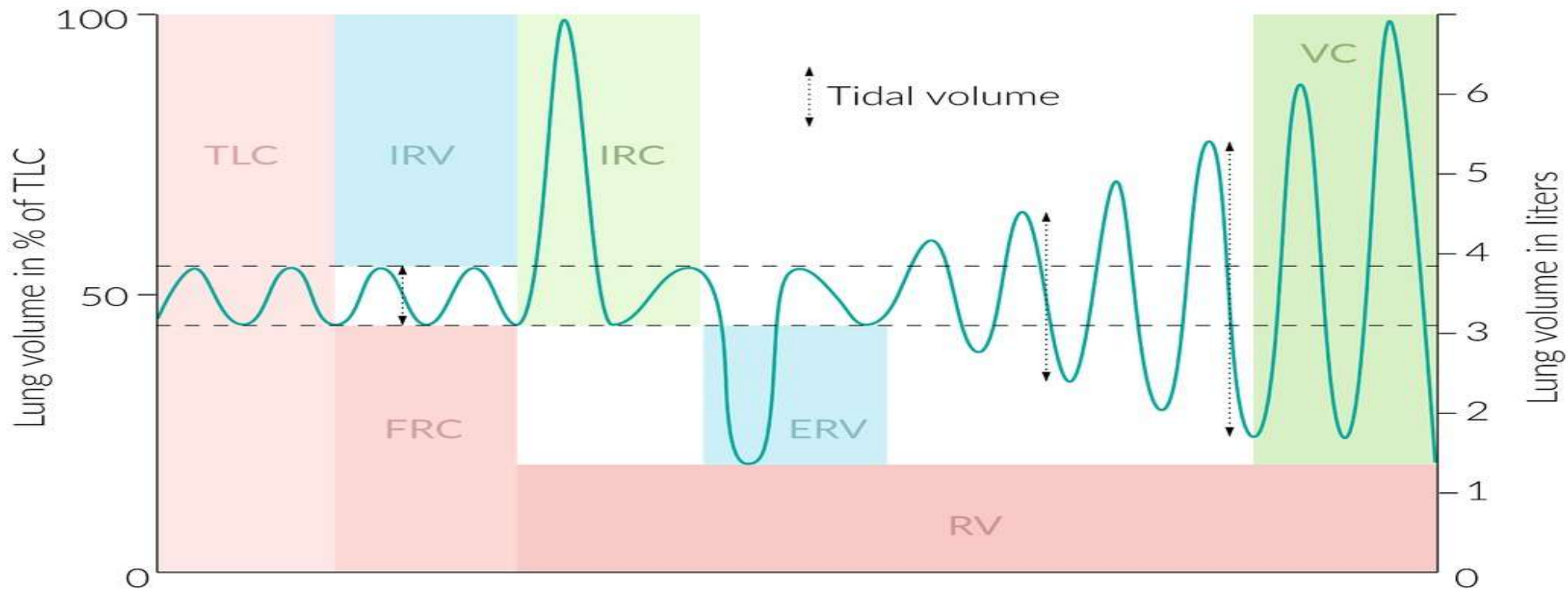
**Bohr equation determines the physiologic dead space :  $VD = V_T \times (P_aCO_2 - P_eCO_2) / (P_aCO_2)$**   
**In a healthy lung, VD equals the anatomic dead space (normal value: approx. 150 mL/breath).**

	<b>Measurement</b>	<b>Adult male average value</b>	<b>Adult female average value</b>	<b>Description</b>
<b>Respiratory volumes</b>	Tidal volume (TV)	500 ml	500 ml	Amount of air inhaled or exhaled with each breath under resting conditions
	Inspiratory reserve volume (IRV)	3100 ml	1900 ml	Amount of air that can be forcefully inhaled after a normal tidal volume inhalation
	Expiratory reserve volume (ERV)	1200 ml	700 ml	Amount of air that can be forcefully exhaled after a normal tidal volume exhalation
	Residual volume (RV)	1200 ml	1100 ml	Amount of air remaining in the lungs after a forced exhalation
<b>Respiratory capacities</b>	Total lung capacity (TLC)	6000 ml	4200 ml	Maximum amount of air contained in lungs after a maximum inspiratory effort: $TLC = TV + IRV + ERV + RV$
	Vital capacity (VC)	4800 ml	3100 ml	Maximum amount of air that can be expired after a maximum inspiratory effort: $VC = TV + IRV + ERV$ (should be 80% TLC)
	Inspiratory capacity (IC)	3600 ml	2400 ml	Maximum amount of air that can be inspired after a normal expiration: $IC = TV + IRV$
	Functional residual capacity (FRC)	2400 ml	1800 ml	Volume of air remaining in the lungs after a normal tidal volume expiration: $FRC = ERV + RV$

**(b) Summary of respiratory volumes and capacities for males and females**



**(a) Spirometric record for a male**



<b>Lung volume</b>	<b>Definition</b>	<b>Normal range</b>
<b>Total lung capacity (TC, TLC)</b>	<ul style="list-style-type: none"> <li>•Volume of air in the lungs after maximal inhalation</li> </ul> $TC = VC + RV$	•6–6.5 L
<b>Vital capacity (VC)</b>	<ul style="list-style-type: none"> <li>•Difference in lung volume between maximal exhalation and maximal inhalation</li> </ul> $VC = TV + IRV + ERV$	•4.5–5 L
<b>Residual volume (RV)</b>	<ul style="list-style-type: none"> <li>•Volume of air that remains in the lungs after a maximal exhalation</li> </ul>	•1–1.5 L
<b>Tidal volume (TV)</b>	<ul style="list-style-type: none"> <li>•Volume of air that is inhaled and exhaled in a normal breath at rest</li> </ul>	•~ 500 mL or 7 mL/kg
<b>Inspiratory reserve volume (IRV)</b>	<ul style="list-style-type: none"> <li>•Maximum volume of air that can still be forcibly inhaled following the inhalation of a normal TV</li> </ul>	•3–3.5 L
<b>Inspiratory capacity (IC)</b>	<ul style="list-style-type: none"> <li>•Maximum volume of air that can be inhaled after the exhalation of a normal TV</li> </ul> $IRC = IRV + TV$	•3.5–4 L
<b>Expiratory reserve volume (ERV)</b>	<ul style="list-style-type: none"> <li>•Maximum volume of air that can still be forcibly exhaled after the exhalation of a normal TV</li> </ul>	•1.5 L
<b>Expiratory capacity (EC)</b>	<ul style="list-style-type: none"> <li>•Maximum volume of air that can be exhaled after the inspiration of a normal TV</li> </ul> $ERC = ERV + TV$	•2 L
<b>Functional residual capacity (FRC)</b>	<ul style="list-style-type: none"> <li>•Volume of air that remains in the lungs after the exhalation of a normal TV</li> </ul> $FRC = RV + ERV$	•2.5–3 L

## CALCULATION POSSIBILITIES USING THE FORMULAS

- $IC = IRV + TV$       **INSPIRATORY CAPACITY = INSPIRATORY RESERVE VOLUME + TIDAL VOLUME =  $3100 + 500 = 3600$  ml**
- $IC = TLC - FRC$
  
- $FRC = ERV + RV$       **FUNCTIONAL RESIDUAL CAPACITY = EXPIRATORY RESERVE VOLUME + RESIDUAL VOLUME =  $1200 + 1200 = 2400$  ml**
- $FRC = TLC - IC$
  
- $VC = IRV + TV + ERV$       **VITAL CAPACITY = INSP RESERVE VOLUME + TIDAL VOLUME + EXPIRATORY RESERVE VOLUME =  $3100 + 500 + 1200 = 4800$  ml**
  
- $VC = IC + ERV$
- $VC = TLC - RV$
  
- $TLC = IRV + TV + ERV + RV = 3100 + 500 + 1200 + 1200 = 6000$  ml      **TLC = TOTAL LUNG CAPACITY**
- $TLC = IC + FRC = 3600 + 2400 = 6000$  ml
- $TLC = VC + RV = 4800 + 1200 = 6000$  ml

• **Flow = volume / time.**

• **Volume = flow × time.**

• **Pressure = flow × resistance.**

• **Resistance = change in pressure / flow.**

• **Compliance = volume / change in pressure.**

• **Work of breathing = pressure × volume.**

### **Lung compliance**

• **Definition:** the ability of the lungs to distend under pressure

• **Measurement:** change in volume of the lung per unit change in pressure ( $C = \Delta V / \Delta P$ )

**AVR = frequency × (TV – dead space) = Alveolar ventilation rate**

**VE = TV × RR      Minute ventilation = total volume of gas entering lungs per min**

**Minute ventilation = tidal volume × respiratory rate (normal is 4-6 L/min)**

**Tidal volume = alveolar space + dead space.**

**the amount of air breathed per minute, which equals about 6 liters** (about 2 liters stay in the anatomic dead space consisting of the upper airway and the mouth, and 4 liters participate in gas exchange in the millions of alveoli constituting alveolar ventilation).



Overview of normal and pathologic ventilation			
Parameter	Normal	Decreased	Increased
Respiratory rate (RR)	12–20/min	Bradypnea (< 12/min)	Tachypnea (> 20/min)
Tidal volume (VT OR TV)	0.5 L/breath	Hypopnea	Hyperpnea
Minute ventilation (VE)	7.5 L/min	Hypoventilation	Hyperventilation

If alveolar ventilation increases (i.e., hyperventilation), more CO<sub>2</sub> is exhaled and the PaCO<sub>2</sub> decreases.

If alveolar ventilation decreases (i.e. hypoventilation), PaCO<sub>2</sub> increases.

Partial pressure during the respiratory cycle (% of total gas composition)			
Gases	In inspired air <sup>[2]</sup>	In alveoli	In expired air
N <sub>2</sub>	593 mmHg (≈ 79%)	573 mmHg (≈ 75%)	593 mmHg (≈ 79%)
O <sub>2</sub>	160 mmHg (≈ 21%)	104 mmHg (≈ 14%)	116 mmHg (≈ 16%)
H <sub>2</sub> O	3.0 mmHg (≈ 0.5%)	47 mmHg (≈ 6%)	47 mmHg (≈ 6%)
CO <sub>2</sub>	0.3 mmHg (≈ 0.04%)	40 mmHg (≈ 5%)	28.5 mmHg (≈ 4%)
<b>Total of all gases</b>	760 mmHg (= 100%)		

Partial pressure of O <sub>2</sub> and CO <sub>2</sub> across the blood-air barrier		
	In the alveoli	In the pulmonary capillaries
Partial pressure of O <sub>2</sub>	104 mm Hg	40 mm Hg
Partial pressure of CO <sub>2</sub>	40 mm Hg	45 mm

- **Mean pulmonary arterial pressure (mPAP):** normal 10–14 mmHg
- **Pulmonary capillary pressure:** ~ 8 mmHg

Pulmonary vascular resistance (PVR): the resistance offered by the pulmonary circulatory system that must be overcome to create blood flow

$$PVR = \frac{P_{\text{pulm artery}} - P_{\text{L atrium}}}{CO}$$

$P_{\text{pulm artery}}$  = pulmonary artery pressure

$P_{\text{L atrium}}$  = left atrial pressure (pulmonary capillary wedge pressure)

CO = cardiac output

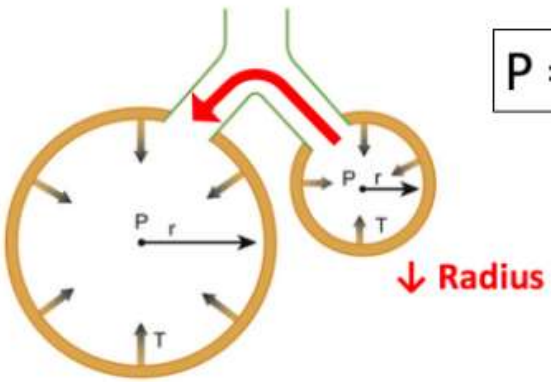
Ventilation-perfusion ratio (V/Q ratio): the volumetric ratio of air that reaches the alveoli (ventilation) to alveolar blood supply (perfusion) per minute

- **Ideal V/Q ratio = 1**
- **Average V/Q ratio = 0.8**
- **At the apex = 3 (V > Q)**
- **At the base = 0.6 (Q > V)**

In an upright position, the lung bases are better ventilated and perfused than the apices (apex of the lung)

Laplace law

↓ Surfactant



$$P = 2T / r$$

↑ Surfactant

